

# Appendix G Worksheet

Directions: Write out the form of the partial fraction decomposition of the function but do NOT determine the numerical values of the coefficients

$$1. \int \frac{2x \, dx}{(x+3)(3x+1)} = \int \frac{A}{x+3} + \frac{B}{3x+1} \, dx$$

$$2. \int \frac{1}{x^3+2x^2+x} \, dx = \int \frac{1}{x(x^2+2x+1)} \, dx = \int \frac{1}{x(x+1)^2} \, dx = \int \frac{A}{x} + \frac{B}{x+1} + \frac{C}{(x+1)^2} \, dx$$

$$3. \int \frac{x^2-x+6}{x^3+3x} \, dx = \int \frac{x^2-x+6}{x(x^2+3)} \, dx = \int \frac{A}{x} + \frac{Bx+C}{x^2+3} \, dx$$

$$4. \int \frac{x-7}{(x-4)^2(2x^2+1)^3} \, dx = \int \frac{A}{x-4} + \frac{B}{(x-4)^2} + \frac{Cx+D}{2x^2+1} + \frac{Ex+F}{(2x^2+1)^2} + \frac{Gx+H}{(2x^2+1)^3} \, dx$$

$$5. \int \frac{6}{x^2(x-1)(4x^2+3)(x^2+1)^2} \, dx = \int \left( \frac{A}{x} + \frac{B}{x^2} + \frac{C}{x-1} + \frac{Dx+E}{4x^2+3} + \frac{Fx+G}{x^2+1} + \frac{Hx+I}{(x^2+1)^2} \right) \, dx$$

$$6. \int \frac{x^4}{(x^3+x)(x^2-x+3)} \, dx = \int \frac{x^4 \, dx}{x(x^2+1)(x-3)(x-1)} = \int \frac{A}{x} + \frac{Bx+C}{x^2+1} + \frac{D}{x-3} + \frac{E}{x-1} \, dx$$