

# Finding derivatives using the definition

Ex. Polynomial

Technique: \* Expand terms & distribute \*

$$f(x) = x^2 - 3x$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{(x+h)^2 - 3(x+h) - [x^2 - 3x]}{h}$$

$$= \lim_{h \rightarrow 0} \frac{x^2 + 2xh + h^2 - 3x - 3h - x^2 + 3x}{h}$$

\* Cancel terms \*

$$= \lim_{h \rightarrow 0} \frac{2xh + h^2 - 3h}{h}$$

\* Factor out an  $h$  & cancel \*

$$= \lim_{h \rightarrow 0} \frac{h(2x + h - 3)}{h} = \lim_{h \rightarrow 0} 2x + h - 3$$

\* Plug in zero for  $h$  \*

$$= \boxed{2x - 3}$$

Ex. Fractions

Technique: \* Put terms in numerator over a common denominator \*

$$f(x) = \frac{1}{2x}$$

$$f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} = \lim_{h \rightarrow 0} \frac{\frac{1}{2(x+h)} - \frac{1}{2x}}{h}$$

$$= \lim_{h \rightarrow 0} \frac{2x - (2x+2h)}{2x(2x+2h)h}$$

\* Cancel terms \*

$$= \lim_{h \rightarrow 0} \frac{-2h}{2x(2x+2h)h} = \lim_{h \rightarrow 0} \frac{-2}{2x(2x+2h)} = \boxed{\frac{-2}{(2x)^2}}$$